

Authoring Online Open Textbooks with MathBook XML

II International Conference on Mathematics Textbooks

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Open Source Publishing

Mathematics on the Web

- The Internet is an amazing thing
- Online Encyclopedia of Integer Sequences
- Also: kitten videos
- Your own:
 - printing press
 - shipping and distribution network
 - marketing (e.g., Google Page Rank)
- If you want to be read, you want your writing on the Internet
- “Any good book is available on the Internet (but maybe not legally)”



- Copyright is a government-granted monopoly
- An open license provides additional freedoms
 - Unlimited copying
 - In perpetuity
 - Modifications for personal use
 - Possibly: the right to distribute modifications
 - “Copyleft”



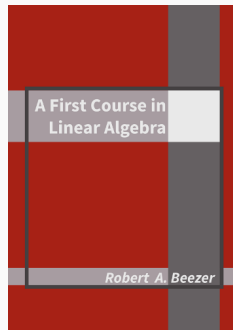
Web Versions of Open Textbooks

- Portable: 64 GB is
 - 64 Encyclopedia Britannica (text)
 - 1 English Wikipedia (text)
 - 10,000 400-page math textbooks
- Ubiquitous: laptop, tablet, or phone
- Up-to-Date: correct, and refresh at will
- Accurate: crowd-sourced proof-reading
- Open: never out-of-print
- Intellectually Honest:
 - no pressure to satisfy market segments
- **FREE!!!!!!**



Sandbox: Open Source Linear Algebra

- A First Course in Linear Algebra
- 2004: Highly structured, semantic \LaTeX
- Distributed as PDF output
- 2006–2008: Rough conversions to HTML
- 2012: Converted source to experimental XML
- 2013: Initiated MathBook XML project
- Today: 500,000 annual unique visits



An Open Textbook, Online

Abstract Algebra: Theory and Applications, by Tom Judson

- #2 in Google “abstract algebra”
- Free! (since it has an open license)
- Hardcopy: \$25

ABSTRACT ALGEBRA DEMONSTRATION



MathBook XML

- An authoring system for all scholarly documents
- Philosophy: **rigorously** separate
 - structure and content
 - presentation

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- Realization: a new source language
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 - XML: eXtensible Markup Language – perfect
 - math content: still \LaTeX (AMS Math)

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- Philosophy: **rigorously** separate
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 - XML: eXtensible Markup Language – perfect
 - math content: still \LaTeX (AMS Math)
- Payoff: multiple outputs from a single source
 - powerful navigation, organization
 - author with your favorite text editor
 - cross-platform open-source toolchain
 - powerful processing with XSL (eXtensible Stylesheet Language)

MathBook XML Technical Example

```
<theorem xml:id="power-rule">
  <title>Power Rule</title>
  <index>power rule</index>

  <statement>
    <p>The derivative of <m> $f(x)=x^n$ </m>
    is <m> $f'(x)=nx^{n-1}$ </m>.</p>
  </statement>

  <proof>
    <p>Apply induction to the product
    <me> $f(x)=x^n=x\cdot x^{n-1}$ </me>
    using <xref ref="product-rule"/>.</p>
  </proof>
</theorem>
```

Theorem 4.4 (Power Rule). *The derivative of $f(x) = x^n$ is $f'(x) = nx^{n-1}$.*

Proof. Apply induction to the product

$$f(x) = x^n = x \cdot x^{n-1}$$

using [Theorem 4.1](#).



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Proof. Apply induction to the product

$$f(x) = x^n = x \cdot x^{n-1}$$

using [Theorem 4.1](#). □

| ≡ Contents | Index | < Prev | ^ Up | Next > |
|-------------------------------------|---|--------|------|--------|
| Front Matter | Theorem 4.4 Power Rule. <i>The derivative of $f(x) = x^n$ is $f'(x) = nx^{n-1}$.</i> | | | |
| 1 Introduction | <i>Proof.</i> | | | |
| 2 The Fundamental Theorem | Apply induction to the product | | | |
| 3 Computing Integrals with Sage (f) | $f(x) = x^n = x \cdot x^{n-1}$ | | | |
| 4 An Interesting Corollary | using Theorem 4.1 . | | | |
| 5 Some Facts and Figures | Corollary 4.5. <i>Suppose $f(x)$ is a continuous function. Then</i> | | | |
| 6 Some Advanced Ideas | | | | |

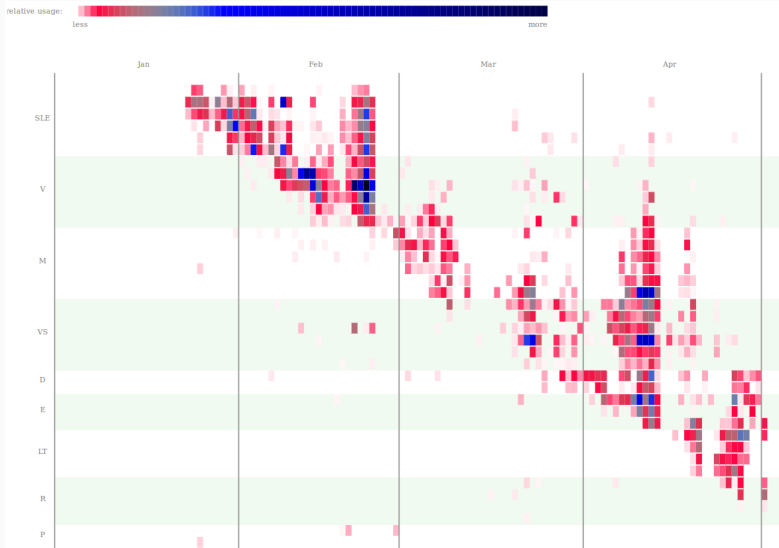
Analyzing Reader Behavior

Analyzing Reader Behavior

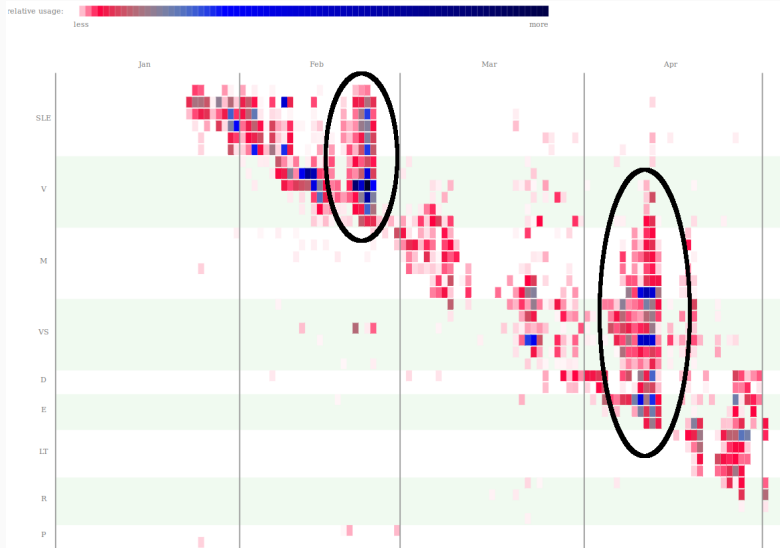
- MathBook XML source is highly **structured**
- Chapter, section, subsection, subsubsection
- Some components require a mouse click to read or use
 - Theorems, plus proof
 - Exercises, plus hints, answers, solutions
 - Cross-references
 - Sage Cells, which are editable
- Which makes it possible to structure the output
- And then we can collect **very fine-grained data**

All Students for Entire Semester

Rows are sections, columns are days



Rows are sections, columns are days



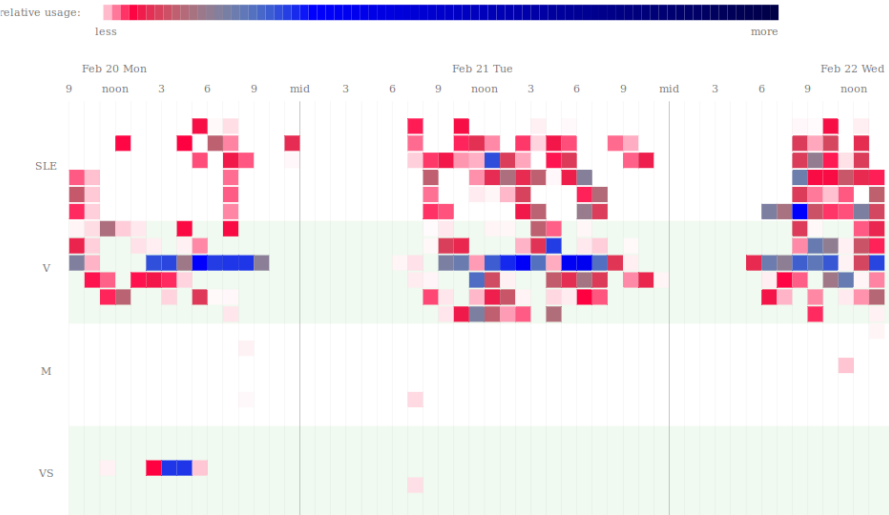
Spring Break!

Rows are sections, columns are days



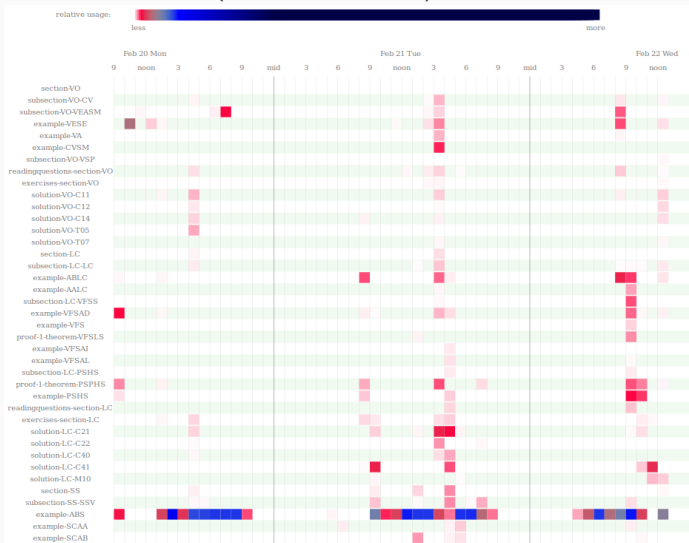
All Students on Tuesday, February 21, 2017

Rows are sections, columns are hours



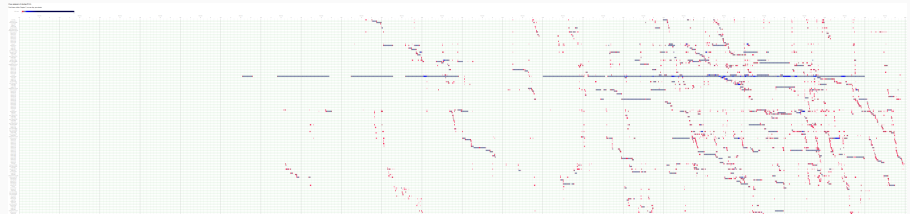
Detail: All Students on Tuesday, February 21, 2017

Rows are components (first third shown), columns are hours



All Students on Tuesday, February 21, 2017, by the Minute

Rows are components, columns are minutes

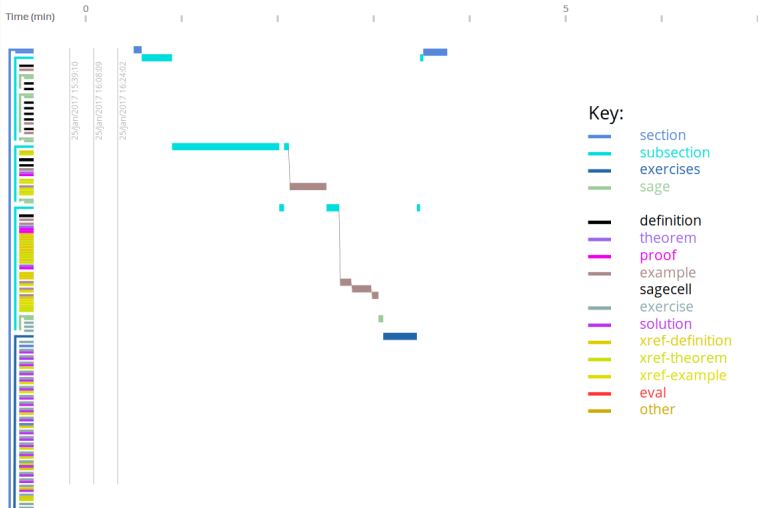


- “Tracks” move down through material, to the right in time
- Denser in the evening — no surprise there

I Like Examples

One student, four minutes, four examples

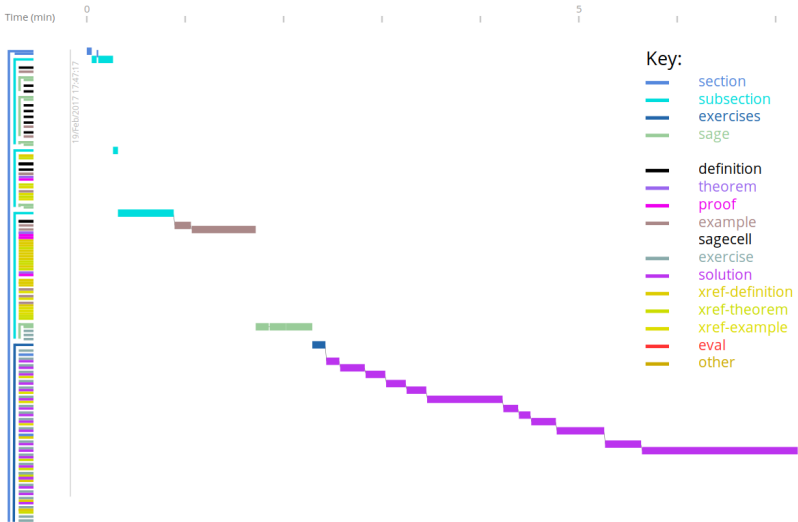
Timeline of viewing [section-RREF](#) by 17.255.236.1.2f704



I Like Solutions to Exercises

One student, seven minutes, two examples, twelve solutions

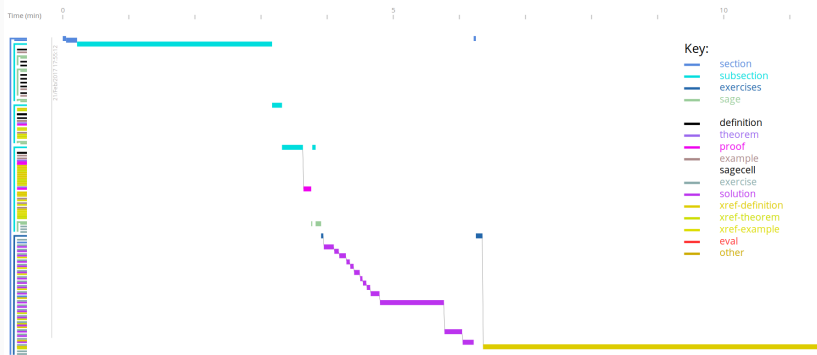
Timeline of viewing [section-RREF](#) by 98.114.47.107.82293



I Like Solutions Too

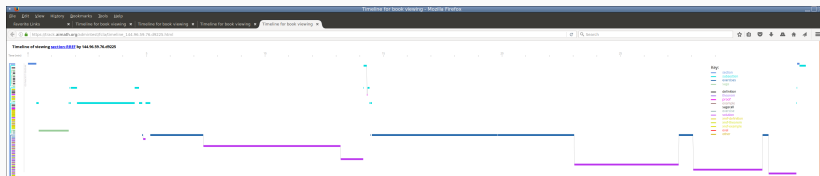
One student, seven minutes plus, first subsection, thirteen solutions, and cross-referenced an earlier definition as a knowl

Timeline of viewing [section-RREF](#) by 216.165.95.69.58c7f



I Like To Study

One student, half an hour, Reading Questions, third subsection, then alternately exercises and solutions



- Data display in web browser
- Tooltips on bars identify content
- Bars are links to actual component of the book
- We can match classroom sessions to student activity

Undergraduate Teaching in Mathematics with Open Software and Textbooks

| | |
|---------------|-----------------------------------|
| Vilma Mesa | U of Michigan |
| Angeliki Mali | U of Michigan |
| Tom Judson | Stephen F Austin State U |
| Susan Lynds | U of Colorado |
| Kent Morrison | American Institute of Mathematics |
| David Farmer | American Institute of Mathematics |
| Rob Beezer | U of Puget Sound |

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`mathbook.pugetsound.edu`

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the author(s) and do not necessarily reflect the views of the National Science Foundation.